

The triangular numbers are given by the following explicit formulas: $T_n = 1 + 2 + \cdots + n = \frac{n(n+1)}{2} = \binom{n+1}{2}$. Here it is proved visually that $\sum_{k=1}^n T_k = \frac{n(n+1)(n+2)}{6}$.