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Strongly bound noncovalent $(\text{SO}_3)_n\text{:H}_2\text{CO}$ complexes ($n = 1, 2$)[†]

Luis Miguel Azofra,^a Ibon Alkorta^a and Steve Scheiner^{*b}

The potential energy surfaces (PES) for the $\text{SO}_3\text{:H}_2\text{CO}$ and $(\text{SO}_3)_2\text{:H}_2\text{CO}$ complexes were thoroughly examined at the MP2/aug-cc-pVDZ computational level. Heterodimers and trimers are held together primarily by $\text{S}\cdots\text{O}$ chalcogen bonds, supplemented by weaker $\text{CH}\cdots\text{O}$ and/or $\text{O}\cdots\text{C}$ bonds. The nature of the interactions is probed by a variety of means, including electrostatic potentials, AIM, NBO, energy decomposition, and electron density redistribution maps. The most stable dimer is strongly bound, with an interaction energy exceeding 10 kcal mol^{-1} . Trimers adopt the geometry of the most stable dimer, with an added SO_3 molecule situated so as to interact with both of the original molecules. The trimers are strongly bound, with total interaction energies of more than 20 kcal mol^{-1} . Most such trimers show positive cooperativity, with shorter $\text{S}\cdots\text{O}$ distances, and three-body interaction energies of nearly 3 kcal mol^{-1} .

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Introduction

Noncovalent bonds,¹ such as hydrogen,^{2–5} halogen,^{6–11} pnictogen^{12–20} or tetrel^{21–24} interactions, act to hold together a wide range of dimers and larger aggregates. They are also essential ingredients in the structure adopted by many single molecules, as they can represent large fractions of the forces between segments that are not covalently bonded to one another. The chalcogen bond^{25–35} is a closely related sort of noncovalent interaction which arises when a member of the chalcogen family (Y), *e.g.* O, S or Se, is drawn toward another electronegative atom (X), made possible in part by the anisotropic distribution of the electron density around Y. These Coulombic attractions are supplemented by charge transfer from the lone pair(s) of the X atom into the σ^* or π^* antibonding Z–Y orbitals (where Z is covalently bonded to Y), which tends to weaken and lengthen the latter Z–Y bond.^{36–39}

Maxima and minima in the molecular electrostatic potential (MEP) represent plausible binding sites for interactions with partner molecules. Minima are typically associated with lone electron pair(s). Maxima can usually be classified into two main groups: (i) σ -holes, which are localized along the extension of the Z–Y bond; and (ii) π -holes, which are situated above the molecular plane.^{37,40–42} O_3 , SO_2 , SO_3 and SeO_2 are a few examples of small molecules that contain π -holes around the central chalcogen atom.^{38,39,43} Understanding the behavior of

these molecules when interacting with other substrates is a fundamental topic, due to their environmental and industrial importance.^{44–48}

Our objective in the present work is a description of complexes containing SO_3 and H_2CO . Both are gases emitted into the atmosphere with severe environmental impact: SO_3 is the main compound involved in acid rain⁴⁴ and H_2CO is the major source of CO due to its photolytic decomposition in higher layers of the atmosphere.⁴⁹ Following a description of the electrostatic properties of the monomers, thorough examination of the entire potential energy surface (PES) of the $\text{SO}_3\text{:H}_2\text{CO}$ heterodimer yields all minima. Careful scrutiny of these minima provides information on the strength and nature of the bonding that holds each together. A number of different minima are then located on the PES of the $(\text{SO}_3)_2\text{:H}_2\text{CO}$ heterotrimer. Their structures are related to that of their parent dimer, and provide information about any cooperativity that might add to their binding strength.

Computational details

The properties of the $(\text{SO}_3)_n\text{:H}_2\text{CO}$ complexes ($n = 1, 2$), were studied through the use of second-order Møller–Plesset perturbation theory (MP2)⁵⁰ with the aug-cc-pVDZ basis set.^{51,52} In all cases, vibrational frequencies were calculated in order to confirm that the structures obtained correspond to true minima. All calculations were carried out *via* the GAUSSIAN09 program (revision D.01).⁵³ Interaction energies, E_{int} , were computed as the difference in energy between the complex on one hand, and the sum of the energies of the two monomers on the other, using the monomer geometries from the optimized complex.

^a Instituto de Química Médica, CSIC, Juan de la Cierva, 3, E-28006, Madrid, Spain

^b Department of Chemistry and Biochemistry, Utah State University, Logan, UT 84322-0300, USA. E-mail: steve.scheiner@usu.edu; Fax: +1 435-797-3390

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The binding energy is defined as the difference in energy between the optimized complex and the sum of the two monomers in their optimized geometries. E_{int} was also corrected by the counterpoise procedure with the monomers in their geometry within the complex.⁵⁴ In order to obtain more accurate values, single point CCSD(T)⁵⁵/aug-cc-pVTZ calculations were performed for the 1 : 1 heterodimers.

The many-body procedure^{56,57} was applied to trimers [eqn (1)] whereby the interaction energy can be expressed as:

$$E_{\text{int}}(\text{trimer}) = \sum \Delta^2 E + \Delta^3 E \quad (1)$$

where $\Delta^n E$ is the n th complex term ($n = 2$ for dimers and 3 for trimers) and the largest value of n represent the total cooperativity in the full complex. Furthermore, E_r , that is, the energy which computes the monomer's deformation, is the link between the interaction (E_{int}) and binding (E_b) energies [eqn (2)], the latter of which is referenced to the fully optimized geometries of the two monomers:

$$E_b = E_{\text{int}} + E_r \quad (2)$$

Atoms in Molecules (AIM)^{58,59} theory at the MP2/aug-cc-pVDZ level, and Natural Bond Orbital (NBO)⁶⁰ analysis with the ω B97XD⁶¹ functional and the aug-cc-pVDZ basis set, were applied to analyze the interactions, using the AIMAll⁶² and NBO6.0⁶³ programs. The appearance of an AIM bond critical point (BCP) between centers of different monomers supports the presence of attractive bonding interactions, which can also be examined by NBO charge transfer between orbitals of different fragments.^{58,64}

The molecular electrostatic potential (MEP) on the 0.001 a.u. electron density isosurface at the MP2/aug-cc-pVDZ level was analyzed for the monomers *via* the WFA-SAS program.⁶⁵ Also, for the heterodimers, the electron density shift (EDS) maps were calculated as the difference between the electron density of the complex and the sum of those of the monomers in the geometry of the complex using the GAUSSIAN09 program (revision D.01).⁵³ Finally, the Localized Molecular Orbital Energy Decomposition Analysis method (LMOEDA)⁶⁶ at the MP2/aug-cc-pVDZ computational level was used to decompose the interaction energy terms *via* eqn (3):

$$E_{\text{int}} = E_{\text{elec}} + E_{\text{exc}} + E_{\text{rep}} + E_{\text{pol}} + E_{\text{disp}} \quad (3)$$

where E_{elec} is the electrostatic term describing the classical Coulombic interaction between the unperturbed electron densities of the two monomers. E_{exc} and E_{rep} are the exchange and repulsive components associated with the Pauli exclusion principle, and E_{pol} and E_{disp} correspond to polarization and dispersion terms, respectively. The dispersion energy refers to the MP2 correction to the Hartree-Fock interaction energy, which contains mainly dispersion and higher-order corrections to the other terms (electrostatic, exchange, repulsion and polarization). These calculations were carried out with the GAMESS program (version 2013-R1).⁶⁷

Results and discussion

Monomers

Sulfur trioxide (SO_3) and formaldehyde (H_2CO) adopt D_{3h} and C_{2v} optimized geometries. Geometries and vibrational frequencies are well described within the MP2/aug-cc-pVDZ level with respect to experimental data: vibrationally averaged structures and anharmonic frequencies.⁶⁸⁻⁷¹ [See Table S1 of the ESI.†] For example, a linear correlation is found between the calculated and experimental frequencies ($R^2 = 0.997$) in Table S1 (ESI†).

Their MEPs on the 0.001 a.u. electron density isosurface are displayed in Fig. 1, where red and blue colors indicate negative and positive regions, respectively. Two ESP minima (grey dots) are associated with each of the O atoms of SO_3 , with values of $-8.85 \text{ kcal mol}^{-1}$, corresponding to the classical "rabbit ear" lone pair directions. Two local ESP maxima (black dots) are located above and below the central S atom, representing very deep π -holes with values of $+52.33 \text{ kcal mol}^{-1}$. H_2CO also exhibits two ESP minima associated with the O lone pairs of the carbonyl functional group, but 3-4 times stronger than those of SO_3 , with values of $-29.18 \text{ kcal mol}^{-1}$. There are ESP maxima along the C-H bond extensions, with values of $+21.84 \text{ kcal mol}^{-1}$, as well as above and below the CH_2 group, with similar values of $+24.72 \text{ kcal mol}^{-1}$.

$\text{SO}_3:\text{H}_2\text{CO}$ heterodimers

Exploration of the full potential energy surface (PES) of the $\text{SO}_3:\text{H}_2\text{CO}$ system at the MP2/aug-cc-pVDZ level led to three minima, whose structures are illustrated in Fig. 2. There appear to be two

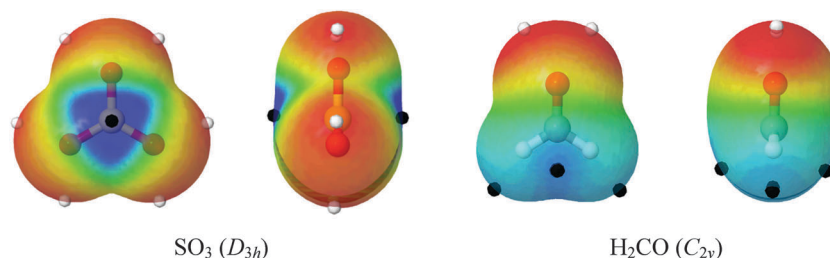


Fig. 1 Molecular electrostatic potential (MEP) on the 0.001 a.u. electron density isosurface for the isolated SO_3 and H_2CO monomers, both calculated at the MP2/aug-cc-pVDZ computational level. The red and blue colors indicate negative and positive regions, respectively, varying between -0.015 and $+0.055$ a.u. for SO_3 , and between -0.040 and $+0.050$ a.u. for H_2CO . Black and grey dots indicate the location of the ESP maxima and minima, respectively, on the surface. Frontal and lateral views are shown for each.

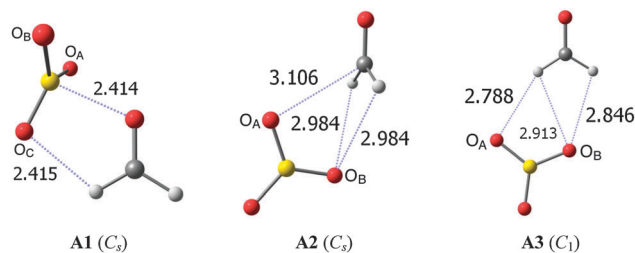


Fig. 2 Structures of the $\text{SO}_3\text{:H}_2\text{CO}$ heterodimers optimized at the MP2/aug-cc-pVDZ computational level. Broken blue lines link atoms which present interatomic AIM BCPs, with interatomic distances in Å. (See Fig. S1 of the ESI† for more complete analysis.) Complexes are arranged in ascending order of energy.

strong and short interactions in **A1**. A chalcogen $\text{S}\cdots\text{O}$ bond with short interatomic distance of 2.414 Å is coupled with a $\text{CH}\cdots\text{O}$ hydrogen bond (HB) of the same length. $\text{CH}\cdots\text{O}$ HBs, albeit much longer ones, are contained in **A2**, along with a long and presumably weak $\text{O}\cdots\text{C}$ interaction (see Fig. S1 of the ESI†). The same two $\text{CH}\cdots\text{O}$ HBs involving both H atoms appear in **A3**, but the $\text{O}\cdots\text{C}$ bond of **A2** is replaced by a third $\text{CH}\cdots\text{O}$ HB; all three of these HBs are rather long. One can draw immediate correlations between the three minima and the electrostatic potentials of the two monomers: **A1** directly connects the deep π -hole of SO_3 with one of the O lone pair minima of H_2CO ; the two H atoms of H_2CO are drawn toward the O_B lone pairs of SO_3 in **A2**; and the O_A lone pair is attracted toward the π -hole of H_2CO . **A3** is stabilized solely by SO_3 O lone pairs and H_2CO H atom attractions.

The interaction energies of the three complexes are reported in Table 1, along with other thermodynamic quantities. It is first evident that **A1** is much more stable than the other two structures, by nearly an order of magnitude. One reason for this distinction can be found in the electrostatic potentials. **A1** combines the deep π -hole of SO_3 with the strong O lone pair minima of H_2CO , while the former π -hole is not involved in **A2** and **A3**. The latter two structures utilize only the O lone pairs of SO_3 , which are much weaker than those of H_2CO (-8.85 vs. -29.2 kcal mol $^{-1}$). The entropy, enthalpy, and free energy values for the formation reactions of the three complexes at $T = 298$ K are also displayed in Table 1. The vibrational corrections to ΔE , both zero point and thermal, lead to less negative values of ΔH , in fact making this

Table 1 Binding, E_b , and interaction, E_int , energies for the $\text{SO}_3\text{:H}_2\text{CO}$ heterodimers at MP2/aug-cc-pVDZ and E_int at CCSD(T)/aug-cc-pVTZ//MP2/aug-cc-pVDZ computational levels. Also, entropy, enthalpy and Gibbs free energy for the association reactions at room temperature (298 K) at MP2/aug-cc-pVDZ computational level. All quantities in kcal mol $^{-1}$, except ΔS , in cal K $^{-1}$ mol $^{-1}$

Dimer	MP2			CCSD(T) ^a		
	E_b	E_int^b	ΔS	ΔH^c	ΔG^c	E_int^b
A1	-11.34	-11.30 (-8.57)	-30.49	-5.92	3.17	-11.70 (-10.52)
A2	-1.85	-1.87 (-0.90)	-15.72	0.33	5.02	-1.56 (-1.06)
A3	-1.72	-1.73 (-0.85)	-13.42	0.38	4.38	-1.57 (-1.11)

^a CCSD(T)/aug-cc-pVTZ//MP2/aug-cc-pVDZ computational level. ^b Counterpoise corrections to basis set superposition error (BSSE) added in parentheses. ^c Counterpoise corrections included.

quantity slightly positive for **A2** and **A3**. Inclusion of the negative entropic factors leads to positive values of ΔG for all three dimers, although **A1** is least positive. Also of note, binding energies are very similar to the interaction energies, a consequence of the very small deformation of the monomer geometries in the complexes (less than 0.04 kcal mol $^{-1}$).

A comparison of SO_3 with SO_2 is of fundamental interest in understanding how the trivalent and divalent molecules differ. An earlier study of the heterodimer of SO_2 with H_2CO found an equilibrium structure very much like **A1** here.³⁸ The $\text{S}\cdots\text{O}$ distance was longer by 0.354 Å, but $R(\text{O}\cdots\text{H})$ nearly the same. Consistent with the longer $R(\text{S}\cdots\text{O})$, the interaction energy of this dimer was 5.42 kcal mol $^{-1}$ at the CCSD(T)/aug-cc-pVTZ//MP2/aug-cc-pVDZ level, only half that of **A1**. Part of this weaker binding for SO_2 can be traced to its shallower π -hole, 31.25 kcal mol $^{-1}$ as compared to 52.33 kcal mol $^{-1}$ for SO_3 . The stronger π -hole in the latter molecule may in turn be attributed to the presence of a third electron-withdrawing O atom.

As two molecules begin to interact with one another, they perturb one another's electron clouds, and these changes can be monitored *via* electron density shift (EDS) maps. The maps in Fig. 3 were calculated as the difference between the electron density of the complex and the sum of the monomers in the geometry of the complex; purple and green regions indicate, respectively, gains and losses of density that arise due to complexation. Consistent with its shorter intermolecular distance and greater interaction energy, the shifts in **A1** are much larger than in **A2** or **A3**, so much so that a smaller isosurface value was necessary to show the more subtle shifts in the latter two dimers. The $\text{CH}\cdots\text{O}$ HBs suggested by AIM in Fig. 2 and Fig. S1 of the ESI† are confirmed by the density shifts, which show the expected density loss around the bridging proton and gain in the lone pair region of the proton acceptor O atom, albeit weaker in **A2** and **A3** than in **A1**. With respect to **A1**, the strong $\text{S}\cdots\text{O}$ chalcogen bond is manifest by green density loss in the region of the S π -hole, and a good deal of purple buildup in the midpoint region between the S and the O. The AIM concept of an $\text{O}\cdots\text{C}$ bond in **A2** corresponds to a density increase in the lone pair region of the corresponding SO_3 O atom, and smaller loss in the π region of C.

Another window into the nature of the interaction arises from a dissection of the total interaction energy into its component parts.

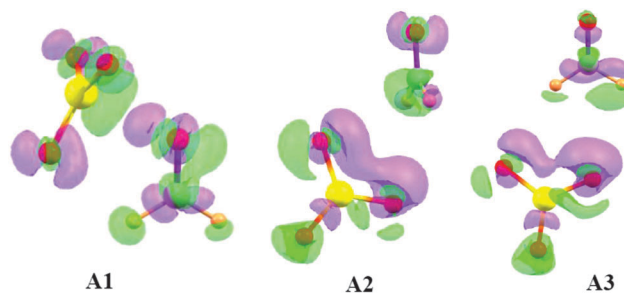


Fig. 3 Electron density shifts (EDS) for the $\text{SO}_3\text{:H}_2\text{CO}$ heterodimers calculated at the MP2/aug-cc-pVDZ level. Purple and green refer to gain and loss of density, respectively, relative to isolated monomers. The values of the isosurfaces are ± 0.002 a.u. for **A1**, and ± 0.0002 a.u. for **A2** and **A3**.

Table 2 LMOEDA energy components, in kcal mol⁻¹, for the SO₃:H₂CO heterodimers calculated at the MP2/aug-cc-pVDZ level

Complex	E_{elec}	E_{exc}	E_{rep}	E_{pol}	E_{disp}	E_{int}
A1	-21.88	-27.37	52.75	-13.46	-1.80	-11.76
A2	-0.86	-2.93	4.89	-0.70	-2.27	-1.87
A3	-1.05	-2.26	3.80	-0.59	-1.63	-1.73

Table 3 Second-order perturbation NBO energy, $E(2)$, in kcal mol⁻¹, for the SO₃:H₂CO heterodimers at ω B97XD/aug-cc-pVDZ computational level, above threshold of 0.5 kcal mol⁻¹

Complex	Donor/acceptor	Type	$E(2)$
A1	H ₂ CO/SO ₃	O _{lp} → π*(SO _A)	34.45
	H ₂ CO/SO ₃	O _{lp} → π*(SO _B)	2.07
	H ₂ CO/SO ₃	O _{lp} → π*(SO _C)	0.99
	SO ₃ /H ₂ CO	O _{clp} → σ*(CH)	1.52
A2	SO ₃ /H ₂ CO	O _{Alp} → π*(CO)	0.84
A3	SO ₃ /H ₂ CO	O _{Alp} → σ*(CH)	0.68

This decomposition was carried out *via* the LMOEDA scheme, and the results are presented in Table 2. For all three structures, the repulsion term is the largest in absolute value. Of the various attractive terms, exchange is the most important, followed by electrostatic and polarization for **A1**, and much smaller, dispersion. Exchange is also the largest component in **A2** and **A3**, but dispersion takes second place, followed by electrostatic and polarization.

NBO analysis is particularly adept at identifying particular charge transfers from one molecular orbital to another. The results of such analysis at the ω B97XD/aug-cc-pVDZ level are reported in Table 3. Considering first **A1**, the dominant transfer, amounting to 34.45 kcal mol⁻¹, occurs from H₂CO O lone pairs to the S–O_A π* antibonding orbital, consistent with the concept of a S···O chalcogen bond as a primary driving force for complexation. There are also minor contributions into other SO π* antibonds, involving O_B and O_C. The O_{lp} → σ*(CH) transfer is typical of what is expected for a CH···O HB; note the much smaller contribution of this HB as compared to the S···O chalcogen bond. The O···C AIM bond of **A2** corresponds to the O_{Alp} → π*(CO) transfer, although the CH···O HBs predicted by AIM for this dimer do not appear in Table 3. While three such CH···O HBs appear in Fig. 2 and Fig. S1 of the ESI,[†] only one such bond (the shortest) is predicted by NBO.

(SO₃)₂:H₂CO heterotrimers

The PES for the (SO₃)₂:H₂CO heterotrimer was explored following a dual strategy: (i) the introduction of a second SO₃ monomer to the SO₃:H₂CO minima taking into account their ESP stationary points; and (ii) fresh initial structures chosen by random selection⁷² were optimized in order to ensure full coverage of the entire PES. The seven most stable minima, which represent essentially the totality of the Boltzmann population are displayed as **B1** to **B7** in Fig. 4. All of these geometries are offshoots of the **A1** dimer, with H₂CO and SO₃(1) similarly disposed. With the sole exception of the symmetric **B6** complex (*C_{2v}*), all trimers have an

important characteristic: the S···O bond between SO₃(1) and H₂CO is shorter than it is in **A1** (2.414 Å). See Fig. 2. This contraction varies between 0.125 Å in **B1** and 0.081 Å in **B7**. In addition to the S···O bond, complexes **B1–B4** and **B7** also contain the secondary CH···O_C HB. $R(\text{H}\cdots\text{O})$, which is 2.415 Å in dimer **A1**, is also reduced in these complexes, by 0.051 Å (**B4**) to 0.016 Å (**B7**).

With respect to the disposition of the two SO₃ monomers within the ternary complexes, the S of the additional molecule SO₃(2) engages in a S···O bond to SO₃(1) in all seven structures. This interaction is augmented by an O···C bond to the H₂CO in **B1–B5**. The latter distance averages 2.862 Å, shorter by 0.244 Å than the O···C distance in the **A2** heterodimer. This contraction indicates enhancement of the electrophilic character of the C atom due to the presence of SO₃(1) and the S···O bond in which it engages. In several of the dimers, *viz.* **B2**, **B4**, **B5**, and **B7**, the two SO₃ molecules form an O···O chalcogen bond. Symmetric **B6** differs in that both SO₃ monomers are situated as in **A1**. As the central H₂CO acts as double electron donor in two S···O bonds, it is not surprising to note that the $R(\text{S}\cdots\text{O})$ distance in **B6** is 0.114 Å longer than in **A1**; likewise for the 0.105 Å longer CH···O HBs. The absence of such O···O bonds in the dimers of Fig. 2 is likely due to the Coulombic repulsions between negatively charged regions that surround these atoms. This negative charge is more intense in H₂CO, so its O atom avoids O···O interactions in both dimers and trimers. The weaker negative region around the O atoms of SO₃ permits a certain degree of O···O bonding, albeit weaker, in the trimers. Note for example, that there is no $R(\text{O}\cdots\text{O})$ intermolecular distance in Fig. 4 that is shorter than 3.2 Å.

Results of a many-body analysis for the most stable (SO₃)₂:H₂CO heterotrimers are displayed in Table 4. The three first columns refer to two-body terms, where subscripts 1, 2 and 3 correspond to H₂CO, SO₃ molecule situated as in **A1** [SO₃(1)] and the second SO₃ molecule [SO₃(2)], respectively. It is noteworthy that the quantities obtained for E_{12} in all cases, with the exception of the symmetric **B6** minimum, are more negative than the -11.30 kcal mol⁻¹ obtained for the interaction energy in **A1**, suggesting that the presence of the second SO₃ molecule enhances the bonding between H₂CO and SO₃(1), consistent with the aforementioned shortened S···O distances. The second SO₃ molecule interacts much less strongly with H₂CO (E_{13}) than does the first, presumably due to the absence of a S···O bond between them (with the obvious exception of **B6**).

The three-body term represents the total cooperativity in the full complex. Negative values of Δ^3E are associated with positive cooperativity; that is, formation of each trimer is energetically favored, while positive values of Δ^3E , represent the opposite.⁷³ Negative values of Δ^3E may be noted for all trimers with the exception again of **B6**, with values that vary between -1.02 kcal mol⁻¹ for **B7** up to -2.92 kcal mol⁻¹ for **B2**.

The total interaction energies vary between -19.10 and -22.06 kcal mol⁻¹, categorizing these trimers as very tightly bound. The small differences between the energies of the first few trimers make it difficult to state with certainty which would be most stable at a higher level of theory. On the other hand,

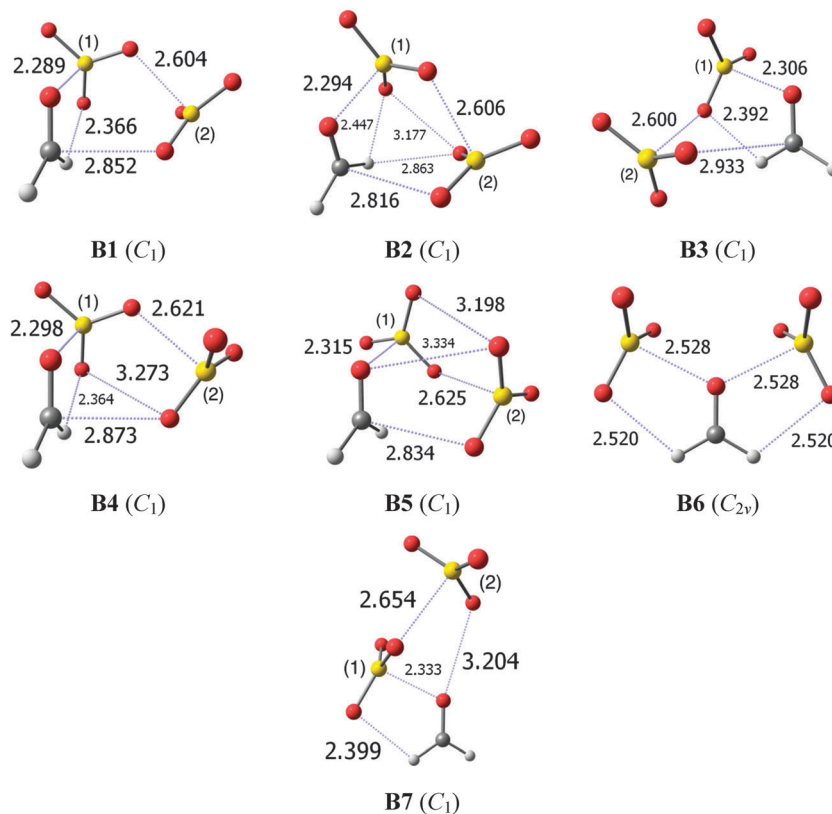


Fig. 4 Most stable structures of the $(\text{SO}_3)_2\text{:H}_2\text{CO}$ PES optimized at the MP2/aug-cc-pVDZ computational level. Broken lines link atoms which present interatomic AIM BCPs, with interatomic distances in Å. (See Fig. S1 of the ESI† for more complete analysis.) Complexes are arranged in ascending order of energy. Index (1) refers to the SO_3 monomer situated as in dimer **A1**.

Table 4 Many-body analysis, in kcal mol^{-1} , for the most stable $(\text{SO}_3)_2\text{:H}_2\text{CO}$ heterotrimers calculated at MP2/aug-cc-pVDZ computational level. Subscripts 1, 2 and 3 refer to H_2CO , SO_3 molecule from **A1** [$\text{SO}_3(1)$], and the second SO_3 molecule [$\text{SO}_3(2)$], respectively

Comp.	E_{12}	E_{13}	E_{23}	$\sum \Delta^2 E$	$\Delta^3 E$	E_{int}	E_r	E_b
B1	-11.82	-2.15	-5.34	-19.31	-2.75	-22.06	2.39	-19.67
B2	-11.60	-2.40	-4.92	-18.92	-2.92	-21.84	2.38	-19.46
B3	-11.94	-1.69	-5.38	-19.01	-2.69	-21.70	2.31	-19.39
B4	-11.82	-2.61	-4.82	-19.25	-2.40	-21.65	2.27	-19.38
B5	-11.54	-2.17	-4.92	-18.63	-2.60	-21.23	2.23	-19.00
B6	-10.52	-10.52	-0.05	-21.09	1.67	-19.42	0.80	-18.62
B7	-11.64	-1.13	-5.31	-18.08	-1.02	-19.10	1.69	-17.41

MP2/aug-cc-pVTZ//MP2/aug-cc-pVDZ calculations for the three most stable trimers indicate that the order remains intact and the energy differences in fact become larger, with relative energies 0.00, 0.38 and $0.56 \text{ kcal mol}^{-1}$, respectively. These results sustain the validity of our methodology. Deformation energies of the monomers needed to conform to the trimer constraints (E_r) are between 0.80 and $2.39 \text{ kcal mol}^{-1}$. Adding this deformation energy to the total interaction leads to the binding energies in the last column of Table 4, preserving the energetic ordering of E_{int} .

As in the case of the dimers, NBO analysis complements the type of information derived from AIM. Table 5 reinforces the idea that the strongest binding force arises from the $\text{S} \cdots \text{O}$

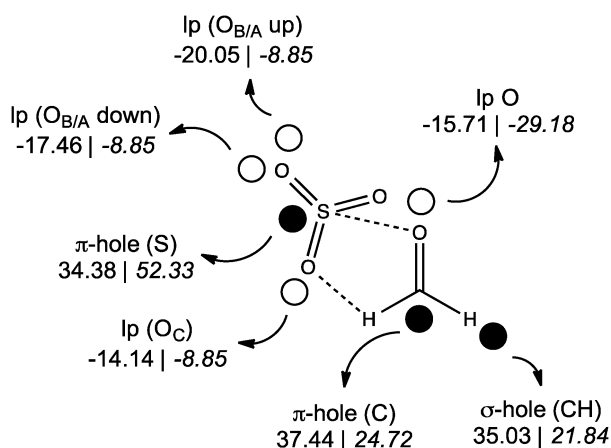
chalcogen bond between $\text{SO}_3(1)$ and H_2CO , with $E(2)$ values between 49.83 and $58.29 \text{ kcal mol}^{-1}$ (for ease of interpretation, all the contributions for a given type of noncovalent bond have been summed: for example, $\text{O}_{\text{Ip}} \rightarrow \pi^*(\text{SO})$ combines $\text{O}_{\text{Ip}} \rightarrow \pi^*(\text{SO}_A) + \text{O}_{\text{Ip}} \rightarrow \pi^*(\text{SO}_B) + \text{O}_{\text{Ip}} \rightarrow \pi^*(\text{SO}_C)$ contributions). Note that this quantity is larger than the same property in the original **A1** dimer, where $E(2)$ was $37.51 \text{ kcal mol}^{-1}$, reinforcing the ideas of positive cooperativity arising from geometries and many-body analysis (again, the **B6** trimer is an exception, with its negative cooperativity). The second largest contribution, on the order of 10.35 – $13.89 \text{ kcal mol}^{-1}$, is associated with the interactions between the two SO_3 molecules, typically another $\text{S} \cdots \text{O}$ chalcogen bond. Much smaller are a range of different tertiary interactions, which include $\text{O}_{\text{Ip}} \rightarrow \sigma^*(\text{CH})$ for $\text{CH} \cdots \text{O}$ HBs, $\pi(\text{CO}) \rightarrow \pi^*(\text{SO})$, and $\text{O}_{\text{Ip}} \rightarrow \pi^*(\text{CO})$.

Relationships between several of the computed properties of the chalcogen bonds in the dimers and trimers were examined, including both those between H_2CO and SO_3 , and those between pairs of SO_3 molecules. For instance the electron density at the bond critical point varies exponentially with $R(\text{S} \cdots \text{O})$, with $R^2 = 0.997$. Likewise the Laplacian at the same bond critical point varies linearly with R , with $R^2 = 0.981$. The NBO second-order perturbation energy $E(2)$ has an exponential dependence on R with $R^2 = 0.992$, a linear dependence on ρ_{BCP} with $R^2 = 0.998$, and a linear relationship with $\nabla^2 \rho_{\text{BCP}}$, $R^2 = 0.998$. These functional dependences are consistent with previous reports in the literature.^{30,34,74}

Table 5 Condensed^a second-order perturbation NBO energy, $E(2)$, in kcal mol⁻¹, for the (SO₃)₂:H₂CO heterotrimers at ωB97XD/aug-cc-pVDZ computational level

Complex	Donor/acceptor	Type	$E(2)$
B1	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	58.29
	H ₂ CO/SO ₃ (1)	π(CO) → π*(SO)	0.63
	SO ₃ (1)/H ₂ CO	O _{lp} → σ*(CH)	1.69
	SO ₃ (2)/H ₂ CO	O _{lp} → π*(CO)	0.50
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	13.89
B2	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	57.02
	H ₂ CO/SO ₃ (1)	π(CO) → π*(SO)	0.81
	SO ₃ (1)/H ₂ CO	O _{lp} → σ*(CH)	0.78
	SO ₃ (2)/H ₂ CO	O _{lp} → π*(CO)	1.39
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	13.64
B3	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	54.33
	SO ₃ (1)/H ₂ CO	O _{lp} → σ*(CH)	1.04
	SO ₃ (2)/H ₂ CO	O _{lp} → π*(CO)	0.73
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	13.17
B4	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	56.38
	H ₂ CO/SO ₃ (1)	π(CO) → π*(SO)	0.56
	SO ₃ (1)/H ₂ CO	O _{lp} → σ*(CH)	1.73
	SO ₃ (2)/H ₂ CO	O _{lp} → π*(CO)	1.04
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	12.15
B5	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	53.95
	H ₂ CO/SO ₃ (1)	π(CO) → π*(SO)	0.52
	SO ₃ (1)/H ₂ CO	π(SO) → π*(CO)	0.52
	SO ₃ (2)/H ₂ CO	O _{lp} → π*(CO)	3.28
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	12.38
B6	H ₂ CO/SO ₃	O _{lp} → π*(SO)	18.88 ^b
	SO ₃ /H ₂ CO	O _{lp} → σ*(CH)	1.54 ^b
B7	H ₂ CO/SO ₃ (1)	O _{lp} → π*(SO)	49.83
	SO ₃ (1)/H ₂ CO	O _{lp} → σ*(CH)	1.08
	SO ₃ (1)/SO ₃ (2)	O _{lp} → π*(SO)	10.35

^a Sum of all the contributions for a given type of noncovalent bond. For example, O_{lp} → π*(SO) may refer to O_{lp} → π*(SO_A) + O_{lp} → π*(SO_B) + O_{lp} → π*(SO_C) contributions. ^b Due to the C_{2v} symmetry, contributions are equal for SO₃(1) and SO₃(2).



Scheme 1 ESP maxima (filled circles) and minima (open circles) in the **A1** SO₃:H₂CO heterodimer. Numerical values, in kcal mol⁻¹, refer to V_{\max} or V_{\min} in the dimer, followed by the same quantity in the isolated monomers (in italics).

A simplified means of understanding the cooperativity relies on consideration of how the formation of the dimer affects the electrostatic potential of each monomer. The values of V_{\max} and V_{\min} in the **A1** dimer are exhibited in Scheme 1, followed by the same quantity in the isolated monomers. For example, the closed circle near the S atom represents the π-hole of SO₃. Formation of the complex with H₂CO reduces V_{\max} from 52.33 down to 34.38 kcal mol⁻¹, making this S atom a less attractive target for a second S···O chalcogen bond. And indeed, there are no trimers in which a single S atom participates in more than one such S···O bond. In contrast, the π-hole of the C atom experiences an intensification, from 24.72 kcal mol⁻¹ in H₂CO to 37.44 in the dimer, now competitive with the S π-hole in **A1**. This strong π-hole helps explain the presence of O···C bonds in many of the trimer structures, much shorter than this same bond in the dimer. Also strengthened by dimerization are the σ-holes along the C–H bond extensions of H₂CO, accounting for the shortening of the CH···O HBs in the trimers. V_{\min} for the O lone pairs on SO₃ becomes more intense upon pairing with H₂CO. Its value in the monomer is -8.85 kcal mol⁻¹, which becomes more negative, to as much as -20.05 kcal mol⁻¹ in **A1**, another factor in the shortening of the CH···O HBs and the O···C bonds. This sort of profile of enhanced ESP maxima and minima has been used to better understand the sequential inclusion of HCN monomers in homo-oligomers.⁷³

Conclusions

Although there are three minima on the SO₃:H₂CO PES, the global minimum is much more stable than are the other two. This dimer is bound by 10.52 kcal mol⁻¹, primarily due to a strong S···O chalcogen bond. The geometry of this dimer places an O lone pair of the H₂CO molecule in close proximity to the positive potential directly above the S atom of SO₃ (a π-hole). There is also a great deal of charge transfer from the former lone pair to the S–O π* antibonding orbital. A smaller contribution arises from a CH···O HB.

When a second SO₃ molecule is added, most of the ensuing heterotrimers contain the structure of the original dimer, and the third molecule placed so that it can interact with both of the original molecules. The latter interactions are varied, but the strongest of these include a S···O chalcogen bond between SO₃ molecules, an O···C bond, O···O chalcogen bond, and a CH···O HB. These trimers are tightly bound, with total interaction energies as high as 22.06 kcal mol⁻¹. Many of the trimer structures show positive cooperativity, with shortened S···O distances, and three-body interaction energies of nearly 3 kcal mol⁻¹.

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