
Exploiting trends in the foreign exchange markets

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We offer further evidence on the relevance of technical trading in exchange-rate markets using daily data for 95 currencies against the US dollar. To that end, we investigate the profitability of a simple technical trading rule based on Taylor's (1980) price trend model, generating optimal one-step-ahead forecasts of returns using genetic algorithms. These trading rules, that bear similarity to the popular trading rules based on moving averages, overcome the buy-and-hold strategy in 25 of 39 cases where trends are detected, even in the presence of transaction costs.

Keywords: exchange rates; price trend model; genetic algorithms; trading rules

JEL Classification: C53; F31; G14

I. Introduction

In the companion paper (Fernández-Pérez *et al.*, forthcoming), we tested for the existence of trends in exchange-rate series for 95 currencies against the US dollar. To that end, we made use of Taylor's (1980) price trend model that concentrates on the short-term pattern of the price trend and, employing a maximum likelihood method and a genetic algorithm to estimate the model, we found evidence in favour of the presence of trends in 39 of the 95 cases considered, with trends more frequent in intermediate exchange-rate regimes.

In this article we undertake the analysis of the profitability of a simple technical trading rule based on Taylor's price trend model. To that end, optimal one-step-ahead forecasts of returns are derived using a genetic algorithm and trading rules based on these forecasts are constructed. We have applied this

investment strategy to daily data on 95 countries from 4 January 1993 to 31 December 2010.

Numerous authors support that, even after taking into account interest rate differentials and transaction costs, standard moving average rules yield excess profits for most of the US-dollar exchange rates. Besides, by using artificial data instead of actual foreign exchange data, this profitability is found to be statistically significant. In this sense, see Dooley and Shafer (1983), Levich and Thomas (1993), Neely *et al.* (1997), LeBaron (1998), Chang and Osler (1999), Gençay (1999), Dewachter (2001) and Harris and Yilmaz (2009), among others.

The rest of this article is organized as follows: Section II presents Taylor's (1980) price trend model. Section III describes the data set and reports our empirical results. Finally, Section IV provides some concluding remarks.

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II. Taylor's Price Trend Model

Taylor's (1980) trend model for a prices time series P_t is defined as

$$\begin{aligned} x_t &= \log(P_t) - \log(P_{t-1}) = \mu_t + \varepsilon_t, \\ E(\varepsilon_t) &= E(\varepsilon_t \varepsilon_{t+i}) = 0, \quad i \neq 0, \quad \text{cov}(\mu_s, \varepsilon_t) = 0 \quad \forall s, t \end{aligned} \quad (1)$$

where the white noise series ε_t is uncorrelated with the stochastic process μ_t representing the trend in the model and it is interpreted as the response to anticipated changes in the supply and demand of the assets. This μ_t may be positive or negative giving rise to increasing or decreasing price trends, respectively. We also define σ^2 as the variance of ε_t , v^2 as the variance of μ_t and $\bar{\mu}$ as the expectation of μ_t .

So, the trend model may be formulated with probability as

$$\mu_t = \begin{cases} \mu_{t-1} & \text{with probability } p \\ \bar{\mu} + \eta_t & \text{with probability } 1 - p \end{cases} \quad (2)$$

where η_t is white noise with mean zero and independent of the past trend values μ_s for $s < t$.

The number of days that the duration of the trend is expected is given by a parameter m (the so-called mean trend duration), and is defined as the averages of the different durations of possible trends

$$m = \sum_{i=1}^{\infty} i(1-p)p^{i-1} = (1-p)^{-1} \quad (3)$$

Omitting technical details which can be found in Taylor and Kingsman (1978), Taylor (1980) and Taylor (2008), the base of the price trend test is the existence of positive correlations between daily rescaled returns x_t/\hat{a}_t with several lags, where \hat{a}_t represents the estimation of the mean absolute deviation which is considered a proxy of the variance of the returns x_t . On the contrary, in the random walk model, all correlations will be 0 for any lag.

The correlations of daily rescaled returns are defined as $\rho_i = \text{cor}(x_t/\hat{a}_t, x_{t+i}/\hat{a}_{t+i})$. Taylor shows that model (1) with μ_t variable as in Equation 2 provides the following correlation expression for rescaled returns:

$$\rho_i = \frac{p^i v^2}{v^2 + \sigma^2} = Ap^i \quad (4)$$

where $A = v^2/(v^2 + \sigma^2)$.

So Taylor (1980) formulated a hypothesis test where the null corresponds to the random walk:

$$H_0 : \rho_i = 0, \quad \text{for each } i > 0 \quad (5)$$

meanwhile, the alternative hypothesis to the random walk model is

$$\begin{aligned} H_1 : \rho_i &= Ap^i, \quad \text{for some } A \geq 0, \\ 0 &\leq p \leq 1, \quad \text{for each } i > 0 \end{aligned} \quad (6)$$

The parameter A is a measure of information that is not instantaneously reflected in the market prices, meanwhile p measures the speed at which the information is reflected in them. If A or p were very close to 0, the information would be used perfectly by the market. But when the trend is accepted, A has a small value, around 3%, and p is close to 1. It means that the market has a slow interpretation of the relevant information that arrives.

Due to the complexity of the log-likelihood function, in order to estimate the parameters, a genetic algorithm is employed (see Dorsey and Mayer (1995) for the use of genetic algorithms for optimizing complex likelihood functions in econometrics). Once the parameters associated with the trend model have been estimated, it is possible to construct technical trading strategies in order to beat the market. We will employ the strategy developed by Taylor (2008) aimed to profit from substantial trends in either direction. This strategy is compounded by three control parameters k_1 , k_2 and k_t where $k_1 > k_2$. The parameter k_1 controls the commencement of trades, telling us when to change a short position for a long position. The parameter k_2 controls the conclusion of the trades, telling us when to change a long position for a short position.

Trading decisions depend on a standardized forecast k_t calculated by assuming the trend model, that is,

$$k_t = \frac{f_{t-1,1}}{\hat{\sigma}_{F,t-1}} \quad (7)$$

where

$$f_{t-1,1} = (\hat{a}_t/\hat{a}_{t-1})\{(p-q)x_{t-1} + qf_{t-2,1}\} \quad (8)$$

$$\hat{\sigma}_{F,t-1} = \hat{a}_t\{Ap(p-q)/(1-pq)\}^{1/2} \quad (9)$$

with $t = 21, \dots, n_{rend}$, where n_{rend} is the total number of returns. In the recursion (8), $f_{t,1}$ is the prediction from an Autoregressive Moving Average model with 1 autoregressive term and 1 moving average term, $ARMA(1,1)$ made in the instant t of the return $t+1$, $\hat{\sigma}_{F,t}$ is its SD, x_t is the no rescaled return of the series in the instant t and \hat{a}_t is the estimated mean absolute deviation.

The Taylor strategy is as follows: we need 20 returns before the beginning in order to estimate the mean

absolute deviations (\hat{a}_t). The values of $f_{t,1}$ and $\sigma_{F,t}$ are assumed to be 0 for $t \leq 20$, and for $t \geq 21$ are estimated recurrently in Equations 8 and 9. After $t \geq 21$, we begin with no market position until $k_t > k_1$ (start a long position) or $k_t < k_2$ (start a short position).

When we are inside the market, if we are in a long position we change to a short position when $k_t < k_2$; if we are in a short position we change to a long position when $k_t > k_1$. For $k_t \in [k_1, k_2]$ do not change the position in any case. When we change our position from long to short or vice versa, a transaction cost of 0.05% is subtracted from the total return. Besides, in order to compute total returns, we assume that, when we are in a short position, the proceeds are invested in a money market account with a risk-free rate of 4% per annum (a year of 252 days is assumed).

In order to select the control parameters k_1 and k_2 , an optimization process is carried out. So, k_1 and k_2 are selected, maximizing the Sharpe ratio of the Taylor strategy in the training period. With that end a genetic algorithm is also employed.

Once the control parameters are estimated they are employed, together with the trend parameters (A , p and q) obtained in the training period, in the prediction period. The net return obtained in the period t to the series i is the following:

$$R_i^t = \sum_{t=21}^{N_{rend}} (x_t buy_t) + \sum_{t=21}^{N_{rend}} [(x_t - riskf_i) sell_t] - c_i mov_t \quad (10)$$

where x_t is the no rescaled return, buy_t stands for a buy signal in the instant t (equal to 1 when we are in a long position and equal to 0 when we are in a short position or we take no market position), c_i is the transaction cost (0.05%), mov_t is the number of times that we change from a short to a long position and vice versa, $riskf_i$ is the risk-free return (4% per annum) and $sell_t$ stands for the sell signals (equal to -1 when we are in a short position and equal to 0 when we are in a long position or we take no market position).

Note that, as technical trading is often criticized on the grounds that the profits generated may be illusory given the existence of transaction costs (see e.g. Korajczyk and Sadka (2004) and Lesmond *et al.* (2004)), we explicitly incorporate such costs in computing the net returns from our trading strategy based on the price trend model.

In order to compare the mean net return of the Taylor strategy with the mean net return of the buy-and-hold strategy, the Sharpe ratio is employed. It divides the net return by its SD, which for the series i in the period t is defined as

$$Sharpe_i^t = \frac{R_i^t / N_{return}}{\sigma_{R_i^t}} \quad (11)$$

where N_{return} represents the number of returns considered in the period.

The buy-and-hold strategy returns are obtained by adding the returns of the series from the first to the last and subtracting two transaction costs corresponding with a buy in the first return and a sale in the last return.

III. Data and Empirical Results

In this article we use daily data of nominal exchange rates against the US dollar for 95 countries from 4 January 1993 to 8 August 2008¹ taken from Reuters' EcoWin Pro.

Given that the countries in our sample present different exchange-rate regimes that could affect the existence of trends, we have used the 'natural fine classification' of Reinhart and Rogoff (2004), updated until December 2010 by Ilzetzki *et al.* (2011), to distinguish between a wide range of *de facto* regimes:

- (1) No separate legal tender
- (2) Pre-announced peg or currency board arrangement
- (3) Pre-announced horizontal band that is narrower than or equal to $\pm 2\%$
- (4) *De facto* peg
- (5) Pre-announced crawling peg
- (6) Pre-announced crawling band that is narrower than or equal to $\pm 2\%$
- (7) *De facto* crawling peg
- (8) *De facto* crawling band that is narrower than or equal to $\pm 2\%$
- (9) Pre-announced crawling band that is wider than or equal to $\pm 2\%$
- (10) *De facto* crawling band that is narrower than or equal to $\pm 5\%$
- (11) Moving band that is narrower than or equal to $\pm 2\%$ (i.e. allows for both appreciation and depreciation over time)
- (12) Managed floating
- (13) Freely floating
- (14) Freely falling
- (15) Dual market in which parallel market data are missing.

Table 1 reports the values of parameters q , k_1 and k_2 for the training period and the returns, obtained in the prediction period (1 January 2008 until 31 December 2010), by both the Buy and Hold (B&H) strategy and

¹ This period differs between series depending on data availability.

Table 1. Parameters of Taylor's strategy and prediction performance statistics

Currencies	Last regime	q	k_1	k_2	B&H	Sharpe-B&H	Taylor	Sharpe-Taylor
Euro	14	0	0	0	0.0081	0.0077	0	0
Algeria dinar	8	0	0	0	-0.0826	-0.0856	0	0
Angola adjusted kwanza	4	0.6288	1.0973	-1.4009	-0.0010	-0.0183	-0.0007	-0.0123
Argentina peso	8	0	0	0	-0.0412	-0.1350	0	0
Australian dollar	13	0	0	0	-0.0218	-0.0168	0	0
Bangladesh taka	7	0	0	0	0.0031	0.0306	0	0
Barbados dollar	2	0	0	0	0.0040	0.0651	0	0
Belize dollar	2	0	0	0	-0.0015	-0.0084	0	0
Bhutan ngultrum	2	0.9316	1.6548	-1.4455	0.1000	0.1710	0.0286	0.0503
Bolivia boliviano	7	0	0	0	-0.0729	-0.1619	0	0
Brazil real	12	0.9759	0.6231	-0.1461	-0.0930	-0.0689	0.1034	0.0896
Brunei Darussalam ringgit	8	0.9822	1.2265	-0.0517	-0.0215	-0.0415	0.0169	0.0351
Burundi franc	8	0.8666	0.7009	-0.1473	0.0581	0.0948	-0.0313	-0.0656
Cambodia riel	7	0	0	0	0.0387	0.0587	0	0
Canada dollar	10	0	0	0	0.0528	0.0488	0	0
Cape Verde escudo	7	0	0	0	-0.0099	-0.0103	0	0
Chile peso	10	0.8431	0.1757	-0.7009	0.0396	0.0271	0.0838	0.0619
China yuan renminbi	4	0	0	0	-0.0670	-0.3056	0	0
Colombia peso	10	0.9833	0.0500	-0.0252	-0.0610	-0.0371	0.1024	0.0650
Congo Democratic Republic franc	13	0	0	0	0.0080	0.0181	0	0
Costa Rica colón	7	0.9924	0.0653	-1.6908	0.1110	0.1989	0.1093	0.2023
Dominican Republic peso	12	0	0	0	0.0504	0.1180	0	0
Ecuador sucre	14	0	0	0	0.0000	0.0000	0	0
Egypt pound	4	0	0	0	-0.0272	-0.0667	0	0
El Salvador colón	1	0	0	0	-0.0007	-0.1559	0	0
Equatorial Guinea ekwele	2	0	0	0	-0.0258	-0.0608	0	0
Ethiopia birr	7	0	0	0	0.0564	0.1722	0	0
Fiji dollar	10	0	0	0	-0.0147	-0.0176	0	0
Gambia dalasi	8	0.9044	1.2286	-0.3230	0.0461	0.0301	0.1944	0.1831
Ghana new cedi	8	0.8884	1.1623	-1.6024	0.1150	0.3954	0.1053	0.3615
Guinea franc	10	0	0	0	0.0588	0.0720	0	0
Guinea-Bissau escudo/peso	15	0	0	0	0.0000	0.0000	0	0
Guyana dollar	7	0	0	0	0.0062	0.0143	0	0
Haiti gourde	12	0.9075	0.6771	-0.9062	0.0708	0.1696	0.0482	0.1417
Honduras lempira	7	0	0	0	0.0038	0.0105	0	0
Hong Kong dollar	2	0.8182	1.9221	-0.8663	0.0000	0.0002	0.0144	0.2278
India rupee	8	0.9336	0.4619	-0.0105	0.1010	0.1394	0.0681	0.0965
Indonesia rupiah	12	0.8412	0.6069	-0.0118	-0.0263	-0.0608	0.0415	0.1058
Israel new shekel	10	0.9012	0.8238	-0.1280	-0.0762	-0.0495	-0.0207	-0.0142
Jamaica dollar	7	0.4626	1.9914	-0.6054	0.0174	0.0658	0.0143	0.1173
Japan yen	13	0.9191	0.6894	-0.0358	-0.0195	-0.0155	-0.0865	-0.0730
Jordan dinar	4	0	0	0	-0.0006	-0.0039	0	0
Kazakhstan tenge	8	0.8926	0.4669	-0.2301	-0.0084	-0.0680	-0.0019	-0.0164
Kenya shilling	8	0.4322	1.2435	-0.4127	0.0716	0.0333	-0.0728	-0.0483
South Korea won	12	0.8258	1.6384	-0.0429	0.1460	0.1229	0.0842	0.0719
Kuwait dinar	4	0	0	0	-0.0232	-0.0704	0	0
Kyrgyzstan som	8	0.9287	0.6811	-0.1067	-0.0215	-0.0313	0.0508	0.0774
Lebanon pound	2	0	0	0	-0.0042	-0.0504	0	0

(Continued)

Table 1. Continued

Currencies	Last regime	q	k_1	k_2	B&H	Sharpe–B&H	Taylor	Sharpe–Taylor
Lesotho loti	2	0.9804	0.5634	−0.0718	0.1361	0.0672	−0.0714	−0.0421
Madagascar ariary	12	0.9669	0.8699	−0.1247	−0.0896	−0.1461	0.0925	0.1574
Malawi kwacha	7	0	0	0	0.0222	0.0558	0	0
Malaysia ringgit	8	0	0	0	0.0206	0.0305	0	0
Maldives Islands rufiyaa	4	0	0	0	0.0124	0.0750	0	0
Mauritania ouguiya	7	0	0	0	−0.0907	−0.1858	0	0
Mauritius rupee	8	0.9914	1.2347	−0.7250	0.0318	0.0355	0.0015	0.0022
Mexico new peso	12	0	0	0	−0.0729	−0.1160	0	0
Moldova leu	8	0.8707	1.0659	−0.1055	−0.1620	−0.4139	0.1689	0.4505
Mongolia tugrik	4	0	0	0	−0.0155	−0.2092	0	0
Morocco dirham	7	0	0	0	5.3454	0.0808	0	0
Mozambique new metical	8	0	0	0	−11.2791	−0.0491	0	0
Myanmar (Burma) kyat	15	0	0	0	0.0000	0.0000	0	0
Namibia dollar	2	0	0	0	0.1273	0.0678	0	0
Nepal rupee	8	0	0	0	0.0980	0.1516	0	0
New Zealand dollar	12	0.9725	0.8684	−0.0735	−0.0907	−0.0671	0.0268	0.0236
Nicaragua cordoba oro	7	0	0	0	−3.3268	−0.0796	0	0
Nigeria naira	12	0.9977	0.8403	−0.1327	−0.0047	−0.0327	0.0163	0.1715
Pakistan rupee	7	0	0	0	0.2013	0.1632	0	0
Papua New Guinea kina	7	0.9674	0.5295	−0.3155	0.0839	0.2011	−0.0080	−0.0193
Paraguay guarani	10	0.6637	1.0996	−0.1296	−0.1766	−0.2685	0.1715	0.2703
Peru new sol	8	0.9843	1.3296	−0.0820	−0.0158	−0.0151	0.0148	0.0148
Philippines peso	8	0.9834	0.2385	−0.0077	0.1000	0.1100	0.0865	0.1015
Qatar riyal	2	0	0	0	−0.0010	−0.0115	0	0
São Tomé and Príncipe dobra	10	0	0	0	0.0362	0.0720	0	0
Saudi Arabia riyal	4	0.9832	1.3994	−0.0360	−0.0007	−0.0097	0.0342	0.4572
Seychelles rupee	8	0.7919	0.0165	−0.0198	0.0009	0.0125	0.0059	0.0855
Sierra Leone leone	4	0	0	0	0.0081	0.0400	0	0
Singapore dollar	11	0.9852	0.6078	−0.4699	−0.0159	−0.0271	0.0537	0.0993
South Africa rand	13	0.0486	0.7426	−0.0711	0.1227	0.0620	0.0852	0.0464
Sri Lanka rupee	7	0.0000	1.4485	−0.8164	−0.0091	−0.0692	0.0008	0.0067
Sudan pound	7	0	0	0	0.0234	0.0432	0	0
Suriname dollar	2	0	0	0	−0.0065	−0.0444	0	0
Swaziland lilangeni	2	0	0	0	0.1274	0.0665	0	0
Syria pound	10	0	0	0	−0.0018	−0.0413	0	0
Tajikistan somoni	7	0.9242	0.7146	−0.5408	−0.0144	−0.1930	0.0290	0.4286
Tanzania shilling	10	0	0	0	0.0077	0.0082	0	0
Thailand baht	11	0.9470	1.0524	−0.1202	0.1284	0.0985	0.0399	0.0326
Tonga pa'anga	8	0	0	0	0.0232	0.0261	0	0
Trinidad and Tobago dollar	7	0	0	0	−0.0073	−0.0111	0	0
Tunisia dinar	8	0.9173	1.3829	−1.7782	−0.0015	−0.0017	0.0353	0.0462
United Arab Emirates dirham	2	0	0	0	−0.0011	−0.0699	0	0
British pound	11	0	0	0	−0.0804	−0.0881	0	0
Uruguay peso	8	0.7158	0.1159	−1.1663	−0.1131	−0.2646	0.0222	0.0634
Venezuela bolivar fuerte	15	0	0	0	0.0000	0.0000	0	0
Viet Nam dong	7	0.9845	0.1441	−0.0734	0.0348	0.0878	0.0278	0.0707
Zambia kwacha	13	0	0	0	−0.0610	−0.0439	0	0

Notes: (1) The predictions period ranks from 1 January 2008 until 31 December 2010.

(2) The parameters of Taylor's strategy were obtained through maximizing the Sharpe ratio by a genetic algorithm.

(3) In dark grey, evidence of trend is found at the 5% confidence level, but Taylor's strategy is not able to improve the B&H strategy.

(4) In light grey, evidence of trend is found at the 5% confidence level, and Taylor's strategy overcomes the B&H strategy.

(5) See text for the classification of *de facto* exchange-rate regimes.

Taylor's strategy whose parameters are obtained by means of a genetic algorithm. The Sharpe ratio of both strategies is also reported.

As can be seen in Table 1, for the exchange rates series where the null hypothesis of random walk was rejected at a significant level of 5%, the return obtained by B&H strategy is higher than Taylor's strategy. This lack of predictive power is also confirmed by comparing Sharpe's ratios which are lower for the B&H strategy. Note that for the series where the trend is not accepted, we have not applied Taylor's strategy.

The countries where the null in favour of trend is rejected may be divided into two groups:

- Currencies where Taylor's strategy is not able to improve the B&H strategy, neither in return nor in Sharpe ratios. This happens in 14 of the 39 cases. For these currencies although, in theory, the trends detected could be employed to beat the market, in practice it does not, at least not in the prediction period considered. Taking into account that sufficient large and long-life trends in prices will make a market inefficient, such markets were probably inefficient during the years studied. However, Taylor's strategy is not able to exploit these inefficiencies with predicting purposes during the prediction period.
- Currencies where Taylor's strategy overcomes the B&H strategy, as much in returns as in Sharpe ratios. This happens in 25 of the 39 cases and this behaviour is more frequent in intermediate exchange-rate regimes. These exchange markets were probably inefficient during the years studied, making it possible to exploit slight dependence between returns using Taylor's trend model after the trading period to generate profitable net returns even taking into account transaction costs.

IV. Concluding Remarks

The profitability of technical trading strategies in foreign exchange markets can be explained by a large class of nonlinear prediction rules potentially deriving from nonlinear versions of structural models such as chaos models by Gilmore (1993), target-zone models by Krugman (1991), monetary model by Meese and Rose (1991), self-exciting threshold autoregressive model by Krager and Kugler (1993), Autoregressive Conditional Heteroskedasticity (ARCH) models by Diebold and Pauly (1988) or Markov switching models by Dewachter (2001). Although these models fit in-sample the data with acceptable level, out-of-sample

tests of these models indicate that their short-term forecasts have little success with respect to the random walk model. In contrast, this article provides additional evidence that trading strategies without theoretical foundation are able to improve the predictions of the random walk model, even taking into account the existence of transaction costs. So, the success of technical trading rules in the foreign exchange market constitutes a major puzzle in international finance.

We believe that our article contributes to the literature by applying a methodological innovation as well as our findings of the presence of economically exploiting trends in exchange rates for a wide sample of countries and exchange-rate regimes.

The results in this article indicate that there exists potential for investors to generate excess returns in exchange-rate markets by adopting technical trading rules-based one-step-ahead forecasts of returns produced by Taylor's (1980) price trend model. In particular, we find that Taylor's strategy overcomes the buy-and-hold strategy in 25 of the 39 cases where trends are detected, even in the presence of transaction costs.

Therefore, this article has showed the potential usefulness of Taylor's price trend model for technical trading rules to forecast daily exchange data when the model parameters are estimated by maximum likelihood using genetic algorithms.

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